## **Challenges in Web Information**

## Retrieval

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## **Statistics for March 2008**

20% of the world population uses the internet [internetworldstats.com]

~300 million searches per day [Nielsen NetRatings]

Search engines are the second largest application on the web

#### World Internet Penetration Rates March 2008







### Search engine architecture

• Open problem: Loadbalancing

### Large-scale distributed programming model

• Open problem: Relationship to data stream model

### **Sponsored search auctions**

• Open problem: Realistic user modeling









All web pages are numbered consecutively

For each word keep an ordered list (posting list) of all positions in all document



⇒ query running time linear in length of posting lists of query terms





## **Query Data Flow**



Split document set into subsets

Place complete index for one or more subsets on each index server

### **Problems**:

- Some servers might have more indices than others
- Some indices have lower throughput than others causing their servers to become bottlenecks



## Idea: Copy Indices



### **Questions**:

Which indices to copy?

How to assign indices and copies to machines?

Where to send individual requests?

⇒ Offline file layout & online loadbalancing problem





### Offline layout phase:

- Set m<sub>1</sub> ... m<sub>m</sub> of identical machines, each has s<sub>i</sub> slots s.t. each indices fits into each slot
- Set  $f_1 \dots f_n$  of indices
- Assign files and copies to machines

Online loadbalancing phase: A sequence of requests arrives s.t.

- every request *t* needs to access one index  $f_i$  and
- places a load of *l*(*t*) on the machine that it is assigned to





Machine load  $ML_i$  = sum of loads placed on  $m_i$ 

**Goal:** Minimize max<sub>i</sub> ML<sub>i</sub> (makespan)

- A(s) = maximum machine load on sequence s
- OPT(s) = maximum machine load on sequence s for optimum offline algorithm that might use a different file layout

**Competitive Analysis**: An algorithm A is **k-competitive** if for any sequence s of requests

$$A(s) \le kOPT(s) + O(1)$$

Goal: Study tradeoff between competitive ratio and number of used slots



### Parameters

### Set $\alpha$ s.t. $\forall i, j: FL_i \leq (1+\alpha)FL_j$ where $FL_i$ = sum of loads of requests for index $f_j$



Set  $\beta$  = max<sub>t</sub> individual request load I(t) Note: In web search engines:  $\alpha$  is < 1,  $\beta$  is constant





### Assumption: Every machine has same number of slots

Slots	n	nm	$\frac{nm}{g(m)} \ge n$	$\frac{3n}{2}$
Competitive ratio deterministic	$1 + \left(1 - \frac{1 + \alpha}{m + \alpha}\right)\alpha$	1	$\star 1 + \left(1 - \frac{1 + \alpha}{g(m) + \alpha}\right) \alpha$	
Competitive ratio randomized				$1 + \frac{\alpha}{2}$ *

\*: some additional conditions apply





## **Open questions**

### Lower bounds

Different models:

- Performance measures
- Machine properties:
  - Speeds (related/unrelated machines)
  - Slots per machine
- Arrival times and duration





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## What is MapReduce?

## System for distributing batch operations over many data items over cluster of machines

### Map phase:

- Extracts relevant information from each data item of the input
- Outputs (key, value) pairs

### Aggregation phase:

• Sorts pairs by key

### Reduce phase:

• Produces final output from sorted pairs list

User writes two simple functions: map and reduce. Underlying library takes care of *all* details

⇒ frequently used within Google (70k jobs in 1 month)





Massive unordered distributed (mud) model of computation:

A mud algorithm is a triple ( $\Phi$ , +, $\Gamma$ ), where

- $\Phi: \Sigma \to Q$  maps an input item to message
- the aggregator +:  $Q \rightarrow Q$  maps two message to a single message
- post-processing operator  $\Gamma: Q \to \Sigma$  produces the final output

For input  $\mathbf{x} = x_1, \dots x_n$  it outputs

$$m(\mathbf{x}) = \Gamma(\Phi(x_1) + \Phi(x_2) + ... + \Phi(x_n))$$

A mud algorithm computes a function f if for all  $\mathbf{x}$  and all possible topologies of + operations:

$$f(\mathbf{x}) = m(\mathbf{x})$$





**Observation**: Any mud algorithm can be computed by a streaming algorithm with the same time, space, and communication complexity.

### Inverse:

• f must be order invariant on input, since mud works on unordered data

**Theorem**: For any order-invariant function f computed by a streaming algorithm with

 g(n)-space and c(n)-communication s. t. g(n)=Ω(log n) and c(n)=Ω(log n)

there exists a mud algorithm with

•  $O(g^2(n))$ -space, O(c(n))-communication, and  $\Omega(2^{polylog(n)})$  time





More efficient mud algorithm

Multiple mud algorithms, running simultaneously over same input, each aggregating only values with same key

 $\Rightarrow$  closer to MapReduce

Multiple iterations

- Example: Finding near-duplicate web pages using k fingerprints per page:
  - 1 MapReduce with space O(k<sup>2</sup>n)
  - 2 MapReduces with space O(kn)





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### Search: hotel princeton





## **Sponsored Search Auctions**

Advertisers enter bids for keywords.

At query time:

Ranking Scheme: System ranks ads by

- Bid
- Effective bid = bid \* click-through-rate
- 2. Payment Scheme: Charge advertisers only if users click on an ad.
  - Generalized First Price (GFP): Pay what you bid: Advertisers see-saw.

•	Generalized Second Price (GSP):
	Pay what the ad below you bid: stable

**Goal**: Design ranking and payment scheme that makes everybody "happy"

Adv	Bid	Price
Alice	\$0.32	\$0.24
Bob	\$0.24	\$0.17
Carol	\$0.17	\$0.14
David	\$0.14	





## Pay what you bid: Non-stability



Source: Edelman, Ostrovsky, Schwarz: Internet Advertising and the Generalized Second Price Auction: Selling Billions of Dollars Worth of Keywords





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Stability: Bidders reach an equilibrium where it's not in their interest to change bids

Simplicity: Bidders can understand how the price is derived from the bids

Monotonicity: Increasing bid does not decrease position and does not decrease click probability





### **Assumptions**:

- *ca(i)* = click-through rate for ad *i*
- cp(j) = click-through multiplier for position j, <math>cp(j) < cp(j-1)
- Separability: Pr[click on ad i at pos j] = ca(i) cp(j)
- Each bidder *i* has internal value v(i)
  - Expected value at position *j*: *ca(i) cp(j) v(i)*
  - Expected utility at position j: ca(i) cp(j) (v(i) price(j))
- If  $p_i$  is the position for bidder *i* then total expected value =

 $\sum_{i} ca(i) cp(p_i) v(i)$ 

Goal: Maximize total expected value (efficient allocation)

**Observation**: Ranking by decreasing *ca(i) v(i)* maximizes total expected value





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**Recall:** System ranks by effective bid = *ca(i) b(i)* 

System knows only *b(i)* not *v(i)* 

### **Payment scheme:**

- Vickrey-Clarke-Groves (VCG):
  - It's best for bidder *i* to bid *v(i)* ⇒ stable
    ⇒ ranking maximizes total expected value
  - Price depends on "damage caused to the other players" ⇒ not very simple
- GSP:
  - simple, monoton, stable,
  - but bidding v(i) is not usually best ⇒ ranking does not usually maximize total expected value



Above separable user model:

Pr[click on ad i at pos j] = ca(i) cp(j)

 "Pick position according to distribution *cp(j)*. Click on the ad in that position with probability *ca(i)*."

More realistic separable user model:

 "Scan from top down. When you reach an ad, click with probability *ca(i)*. Continue scanning with probability *q(i,j).*"





### Markovian user model:

- Scans ads from top down.
- When reaches ad *i* in position *j*, clicks with probability *ca(i)*.
- Continues scanning with probability q(i,j).

For q(i,j) does not depend on j, Feldman et al.

- give simple algorithm for finding best ranking of ads
  - monoton
- VCG payments resulting auction is stable and maximizes total expected value





Markovian User Model

- Non-VCG pricing: Is there a simple, stable payment scheme in the Markovian User Model?
- User impatience: Analyze the case that q(i,j) depends on both i and j
  Model budgets for bidder (Feldman et al, Borgs et al, Dobzinski et al.)
  Consider a variety of advertiser preferences = utility functions
  - I don't care how much I pay, but I always want slot 3.
  - I'm willing to pay up to \$5 per click, or up to \$1 per impression.
  - My margin is \$1 per click. Give me position that maximizes my profit, i.e. value of clicks minus price paid.
  - Maximize my profit, but never spend more than \$0.50 per click.



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# Happy Birthday, Bob!



