

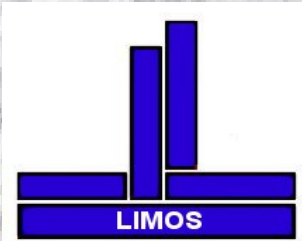
LIMOS

**Laboratoire d'Informatique, Modélisation et
Optimisation des Systèmes
UMR CNRS 6158**

Samuel DELLEPLANQUE, Alain QUILLIOT

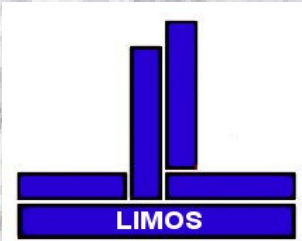
alain.quilliot@isima.fr





SMART CITIES: Old Problems/New Paradigms

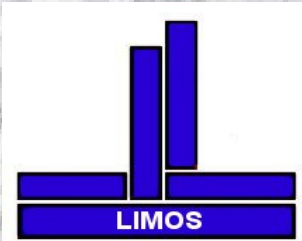
**Classical O.R and New Paradigms:
Innovative Urban/SubUrban Mobility
Of Smart Cities**



Old Problems/New Paradigms: Innovative Mobility

Summary

- I. O.R Trends, New Paradigms**
- II. LIMOS and Innovative Mobility**
- III. A reference problem: Dial/Ride**
- IV. Standard Methods and Benchmarking**
- V. Extensions toward New Contexts**
 - V.1. Mixing Decision Levels**
 - V.2. Non Standard Criteria**
 - V.3. Non Standard Contexts**



Old Problems/New Paradigms

I. O.R Trends, New Paradigms

O.R -> born at the end of the 40's, from the needs of U.S Army;

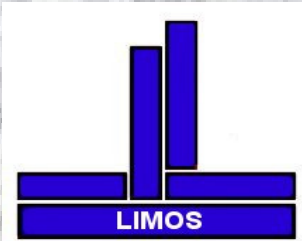
Centralized and static point of view;

Mainframes; High human computing costs;

No web, no P.C, no mobile communication devices

⇒ Linear Programming (Von Neuman/Dantzig) -> Graph Theory (Berge), Complexity (Cook) + MIP (Gomory)

⇒ Polyhedral Theory (Edmonds).



Old Problems/New Paradigms

Year 2010 ?

Many things have changed!

Technology: web services, distributed systems, datamining, mobile communication, high performance computing

Society: democracy requirement, safety, security, environmental concerns

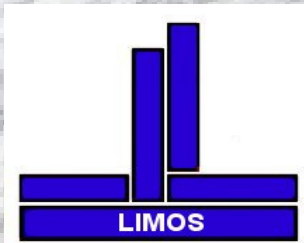
Economics: delocalization, outsourcing, complex supply chain, increasing weight of Finance



New Problems? New way of setting old problems?

Taking into account interactions, safety requirements, economical stability.

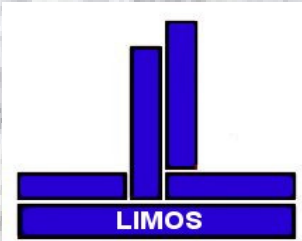
Taking advantage from new technologies.



Old Problems/New Paradigms

=> Extensions toward New Contexts

- **Mixing Decision Levels:**
 - Linking Routing, Pricing and Subsidizing.**
 - Linking Routing and Packing.**
- **Non Standard Performance Criteria:**
 - Robustness and Stochastic Complexity.**
 - Genericity.**
 - Reliability.**
- **Non Standard Contexts:**
 - Collaborative Planning.**
 - Dynamic Scheduling.**



LIMOS: Innovative Mobility

II LIMOS and Innovative Mobility

LIMOS, UMR CNRS/UBP 6158, CLERMONT-FERRAND

- **MAAD: *Decision Models and Algorithms***
- **SIC: *Information and Communication Systems***
- **SP/ROGI: *Production Systems, O.R for Industrial Engineering***
- +
 - **Transversal Actions:**
 - STIC-Mobility*
 - STIC-Environment*
- **LABEX Participations:**
 - Clervolc: Seismic/Volcanic Monitoring**
 - IMOB3: Innovative and Intelligent Mobility**



LIMOS: Innovative Mobility

Partnerships: QUEBEC, HIT HARBIN, UT Compiègne, Centrale LILLE, SNCF...

Related Projects: Managing Decision inside New Generation Mobility Services

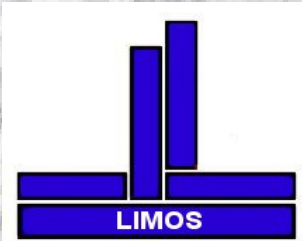
Context: need for more flexibility

- Growth of oil prices

- Environmental issues; City congestion?

- Increasingly old population.

Demand: mixing reactivity with mutualization, taking into account multimodality



LIMOS: Innovative Mobility

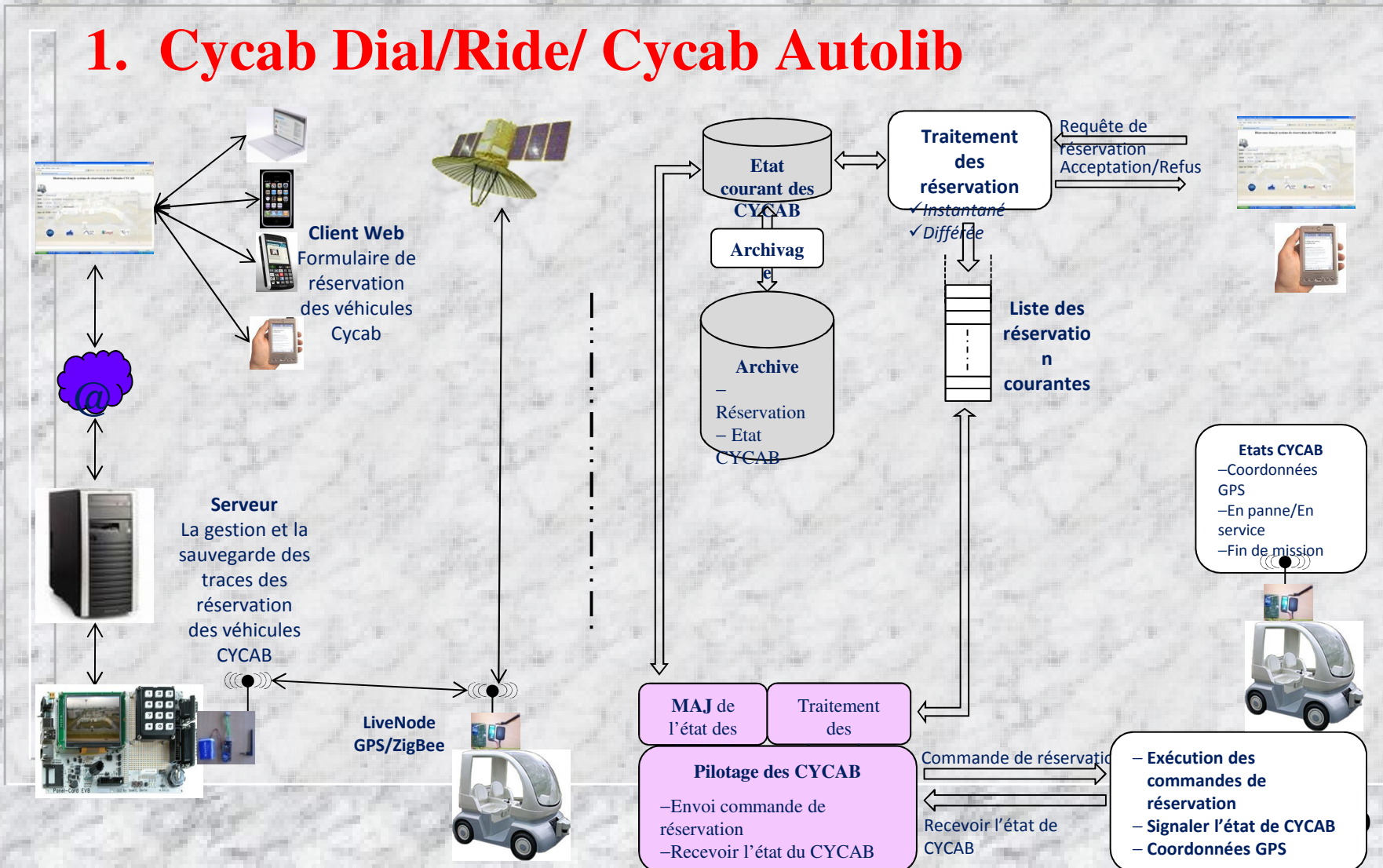
New Generation Mobility Services

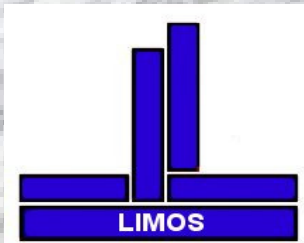
- **CYCAB/VIPA Real Time Dial/Ride**
- **Ad Hoc Shuttle Fleet** management
- **AUTOLIB-Vehicle Sharing** Intelligent Design and Monitoring
- **Intelligent Co-Transportation Systems**
- **Internal Logistics** Optimization



LIMOS: Innovative Mobility

1. Cycab Dial/Ride/ Cycab Autolib



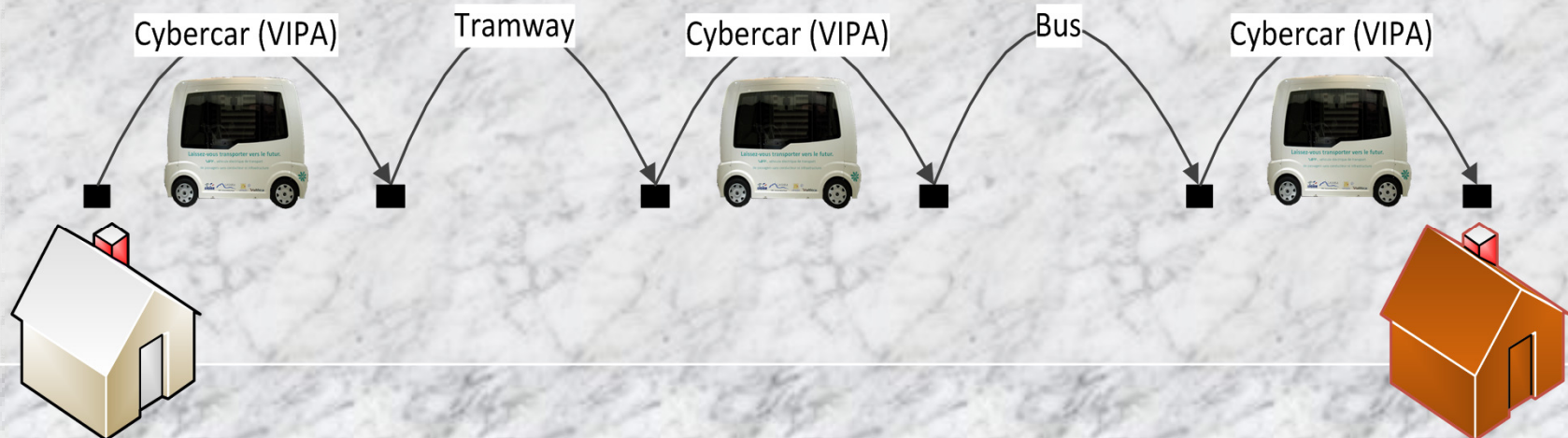


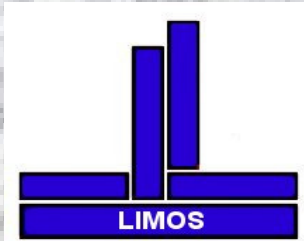
LIMOS: Innovative Mobility

- Used on short distances
- Integration into the intermodal transport of the future

- **Target**

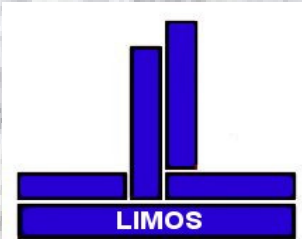
- Large Parking Lots
- Large Factories
- Airports, Train Stations
- Hospitals, Campuses
- Business Centers





LIMOS: Innovative Mobility

- **2 Criteria**
 - **Economic (for the operator) :**
 - Number of used vehicles and total distance,
 - VIPA Load Rate,
 - Number of accident (**reliability**),
 - **Service (for the user) :**
 - Connection speed,
 - Connection success rate (**reliability**).



LIMOS: Innovative Mobility

2. AUTOLIB-Vehicle Sharing Intelligent Design and Monitoring

**VIPA Fleet for AUTOLIB System ->
Relocation through wireless convoys**

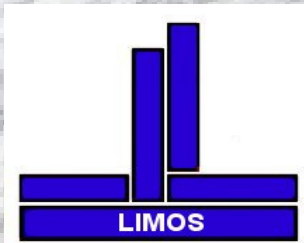
Input: Expected Demand Space-Time Distribution

Output: *Relocation Strategy*.

- *Relocation Signal*: When? .
- *Relocation Process*: how many convoy leaders?
Process Duration? Convoy Routing?
Convoy Making? Inter-Convoy exchanges?

Analogy with *Ambulance Relocation*

(Gendreau, Brotcorne, Laporte, Semet (2003, 2004))



LIMOS: Innovative Mobility

3. Co-Transportation Systems

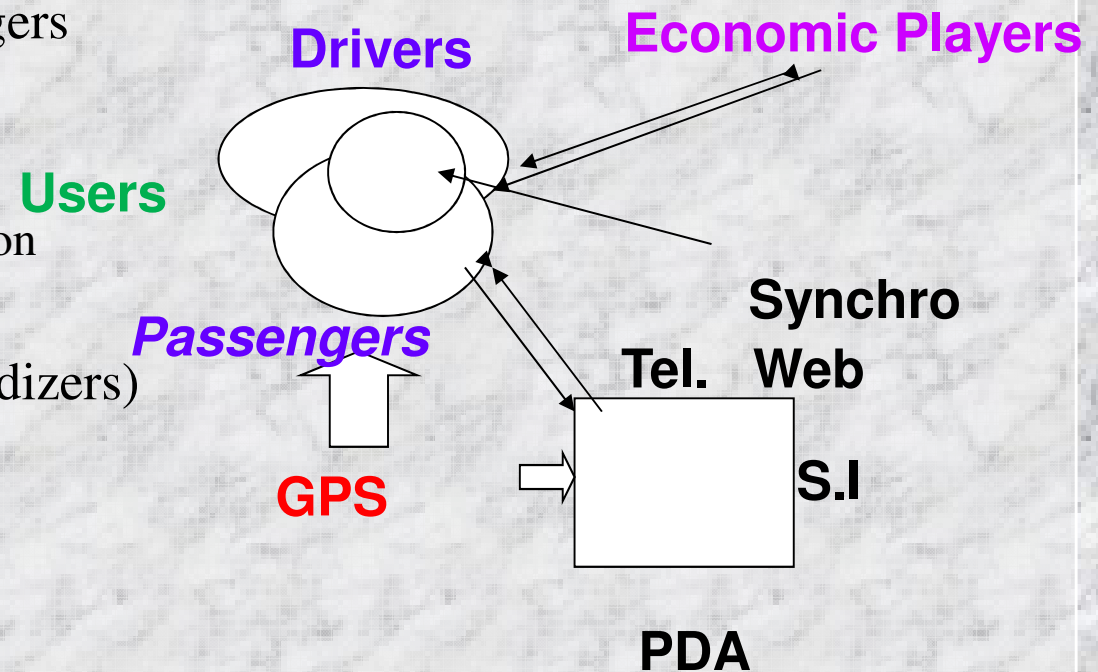
Usagers: drivers and/or passengers

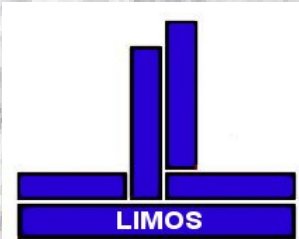
Vehicles (driver owned):

- Simple
- Synchro (ad hoc communication)
- Traceability devices)

Socio-economic players (subsidiizers)

Servicer: intelligent web site +
▪ Geolocalization/Mobile Com.
▪ Infrastructure.





A Reference Problem: DARP

III A Reference Problem: the Dial and Ride Problem (DARP).

Input.

V: Vehicle set; $v \in V \rightarrow C(v) = \text{Capacity characteristics}, S(v) = \text{Speed characteristics}, \Delta(v) = \text{Availability}$

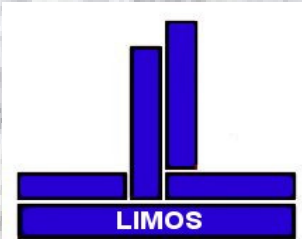
K: Object Set; $C(v)$ is a constraint on integer valued K -vectors

X: Demand Set; $x \in X \rightarrow (o(x), d(x)) = \text{origin/destination pair}, T(x) = \text{Time Window}, D(x) = \text{Load} = \text{Integer valued } K\text{-vector}$

G = (N, A) = Transit Network; $M = \text{Related Shortest Path Distance Matrix}$

Output.

v in $V \rightarrow$ a *timed* route $\Gamma(v)$: every node s in $\Gamma(v)$ is provided with arrive-time, leave-time: time-space, load and unload: X



A Reference Problem: DARP

Output.

v in V \rightarrow a *timed* route $\Gamma(v)$: every node s in $\Gamma(v)$ is provided with arrive-time, leave-time: time-space, load and unload: X

Constraint.

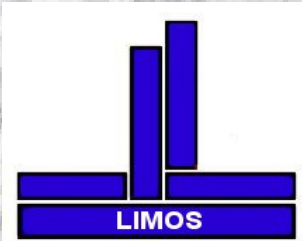
Capacity constraint: at any instant t , current load $L(v, t)$ of vehicle v compatible with capacity constraint $C(v)$

Time windows constraint: any instant demand x is loaded and unloaded according to $T(x)$

Availability Constraint: running time of vehicle v is included into $\Delta(v)$

Speed constraints: for any vehicle v , any consecutive nodes s_1, s_2 in $\Gamma(v)$, arrive-time(v, s_2) – leave-time(v, s_1) is compatible with M and $S(v)$

Load/unload time constraint: for any vehicle v , any node s in $\Gamma(v)$, leave-Time(v, s) – arrive-Time(v, s) compatible with $T(x)$ and $D(x)$, x loaded and unloaded in s .



A Reference Problem: DARP

Performance.

Mix (Multicriterion) = $\text{Card}(\text{Active-Vehicle})$, $\sum_v \text{Length}(\Gamma(v))$,
 $\sum_x \text{Duration}(\Gamma, x)$.

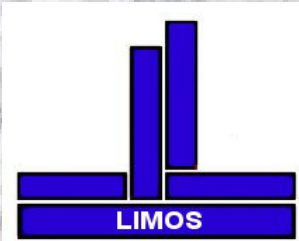
Extensions

- **Vehicle Preemption:** a demand x may be routed from $o(x)$ to $d(x)$ through several vehicles.
- **Load Preemption:** the load $D(x)$ may be split into several sub-loads, which are routed independently.

Static Versus Dynamic .

- Static: all data are known in advance;
- Dynamic: data come as a dataflow; current roadmap of every vehicle is taken into account.

Remark: most often, time windows flexibility is maintained



A Reference Problem: DARP

IV. Standard Methods and Benchmarking.

Simplified Framework: Nodes are splitted according to the demands: any $o(x)$, $d(x)$ is identified with a specific node.

A Simple MIP model (Not Practical...!).

Variables $t = (t_n, n \in N)$, rational, $z = (z_{nm}^v, n, m \in N, v \in V)$ with $\{0, 1\}$ values:

$z_{nm}^v = 1$ means arc (m, n) is part of route $\Gamma(v)$

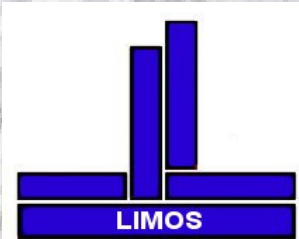
t_n = time at node n , identified with some demand load/unload, is "serviced"

p_n = load at node n , for the vehicle v which services n

Constraints:

- z represents a partition of N into circuits (*Tour Constraints*)
- $\sum_v z_{nm}^v = 1 \rightarrow t_m - t_n \leq M(n, m)$; (*Logical Time Constraints*)
- $\sum_v z_{nm}^v = 1 \rightarrow p_m - p_n = \text{Load}(n)$; (*Logical Load Constraints*)
- $t_{o(x)}, t_{d(x)}, t_{d(x)} - t_{o(x)}$ inside related time windows;
- $p_{o(x)}$ compatible with capacity constraints.

Goal: Minimize $\text{Cost} \cdot z + \sum_x t_{d(x)} - t_{o(x)}$.



A Reference Problem: DARP

Greedy Insertion Scheme:

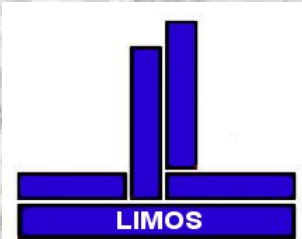
JAW (86), Xiang, Xu, Chen (2006), Toussaint/Quilliot (2010)
Demands are randomly ordered, and inserted according to this order into current partial routes $\Gamma(v)$, v in V
(filtering process through constraint propagation)

Local Search and Metaheuristics scheme (Tabu, Simulated Annealing...)

- Ropke, Cordeau, Laporte (2006): Tabu Heuristics
- Calvo, Colorni (2006): Heuristics Insertion/Assignment
- Psafaratis, Sexton, Bodin (80, 79, 85, 95)

Local operators:

- *Exchange*: 2 demands are exchanged between 2 tours
- *Shift*: 1 demand is shifted from one tour to another one;
- *Internal-Shift*: 1 demand is relocated inside a given tour



A Reference Problem: DARP

Branch/Bound, Branch and Cut:

Ropke, Cordeau, Laporte (2001, 2003);

Exact results up to 25 demands

Branching Process: on the variables z_{nm}^v of the PLNE representation

Bounding process: using the PLNE representation + ad hoc cuts

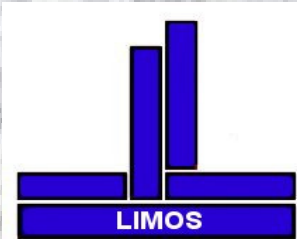
Toussaint/A.Q (2010)

Greedy Insertion + Branch/Bound

Branching Process + Constraint Propagation:

Demand x in tour v ?

Efficient if sharp time window constraints.



A Reference Problem: DARP

Dynamic Flow (Flow over Time):

Recall: Flows/Multicommodity Flows

Network $G = (Z, E)$

Flow $z = E$ (arc) indexed vector such that for every

node x , $\sum_{e \text{ enter } x} z_e = \sum_{e \text{ out } x} z_e$, (Kirshoff Law)

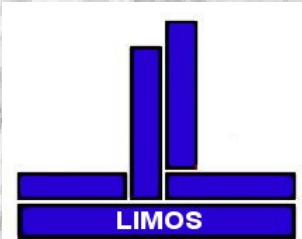
Kirshoff Law may be adapted in order to make z express the routing of a given quantity from one node to another

Multicommodity Flow: collection of flow vectors, whose values identify distinct class of objects

Dynamic Flow Framework: nodes are (pair (n, t) , n in N , t in the time space)

-> *Explicit or implicit representations*

DARP: Vehicle Flow + Multicommodity Demand Flow, tied with coupling capacity constraints (Master/Slave scheme) -> Local operators related to the flow/multicommodity-flow machinery -> Cancelling circuits/cycles (Bauman (2007), Skutella (2006), Fleischer (2000, 2001), Ford/Fulkerson (1962), Martens, Salazar(2007))

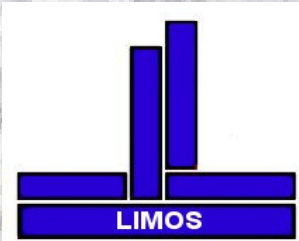


A Reference Problem: DARP

Clustering and Column Generation: Ropke, Laporte (2001, 2003), Desrosiers, Soumis, Dumas (89), Vigo, Toth (96), BERLIN-TELEBUS, Bjorndorfer 97: Clustering.

Column Generation: main vector indexed on the set of all the possible tours -> induced subproblem: Generating efficient tours.

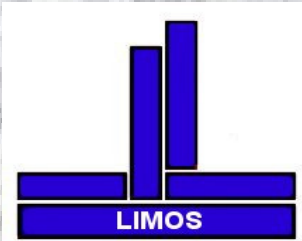
Clustering: **master vector** index on the set of X subsets, i.e: which demands are handled by the same vehicles; **slave object:** the tour related to some subset A of X , which is part of the cluster. **Column generation** -> generating the ad hoc subsets A .



A Reference Problem: DARP

Dynamic Context: (few studies)

- BERLIN-TELEBUS, Bjorndorfer 97: Extraction of Seed Trajectories
- Madsen, Rygaard, Ravn (Copenhagen TAD System, 1995): Adaptation of Jaw Insertion Techniques
- Todorovic, Radijonovic (2000): Application of Fuzzy Logic Rules
- Colorni, Righini (2001): Real Time Clustering through Local Transformation
- Coslovitch, Pesenti, Ukovitch (2006), Fabri (2007): insertion rules + 2-opt like reoptimization heuristics



A Reference Problem: DARP

Remarks about usual dynamic models.

Models: dataflows, algorithms take into account current roadmaps of the vehicles;

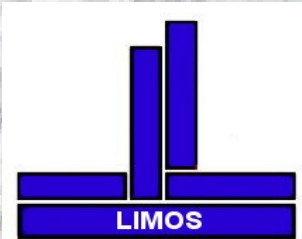
Demands: $n = 25$ to 900, no focus on the real time constraints induced by communication and supervision;

What about taking into account stochastic demand distribution?

Soft management of real constraints: time windows remain open all throughout the process, until the user is serviced.

What about system/user communication and « rendez-vous » mechanism?

Dynamic most often means « perturbation handling »: what about failure (vehicle delay, user give up...)?



A Reference Problem: DARP

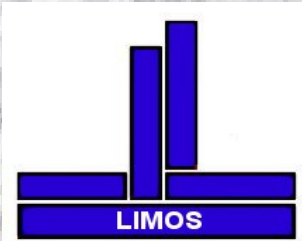
Static/Dynamic DARP: Benchmarking.

TSP LIB, Laporte Cordeau Instances, ... -> Toy Problem -> many academic test beds

A few word about instances generation:

Fagin Theorem: The theoretical values of randomly generated instance with non null density $\{0, 1\}$ of a problem expressed according to the 2 order monadic logic formalism converge almost surely (either to 1 or to 0).

Courcelle Theorem: 2 order monadic logic problems with bounded clique width are time-polynomial



A Reference Problem: DARP

In most cases, testbed instances => generated according to the 2 order monadic logic formalism.

=> **They are strongly biased.**

Experiments -> Testing ad hoc Indicators on common testbeds:

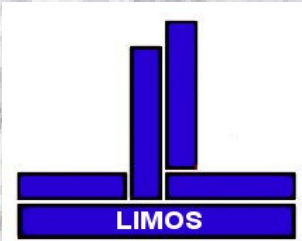
- ⇒ *parallelism rate*: number of demands which may be simultaneously handled;
- ⇒ *Dispersion rate* : variance of $o(x)$, $d(x)$ distribution....

We remark: very concentrated distribution.

⇒ Generating meaningful testbeds is a difficult game.

Example: Cordeau/Laporte instances -> very strong temporal constraints -> getting initial solution is difficult -> advantage to constraint propagation + “repairment” heuristics.

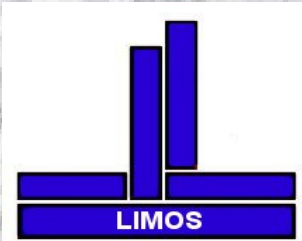
Dynamic Case: what about dataflow generation, and launching of the recomputation process? What has to be measured?



DARP: New Paradigms

V. DARP: New Contexts mean New Paradigms.

- **Mixing Decision Level** (routing/packing, economical management)
- **Non Standard Criterion** (reliability, robustness...)
- **Non Standard Contexts** (collaborative, reactive...)



DARP: New Paradigms

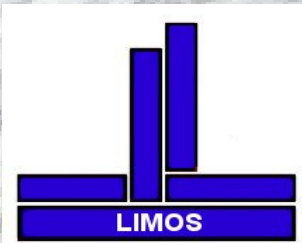
V.1. Mixing Decision Levels.

Linking Routing and Packing: loads are 2D or 3D-objects, with geometrical characteristics -> Non trivial testing of capacity constraints, time consuming loading and unloading operations
-> 3L-CVRPV (Duhamel, Lacomme, Quilliot, Toussaint)

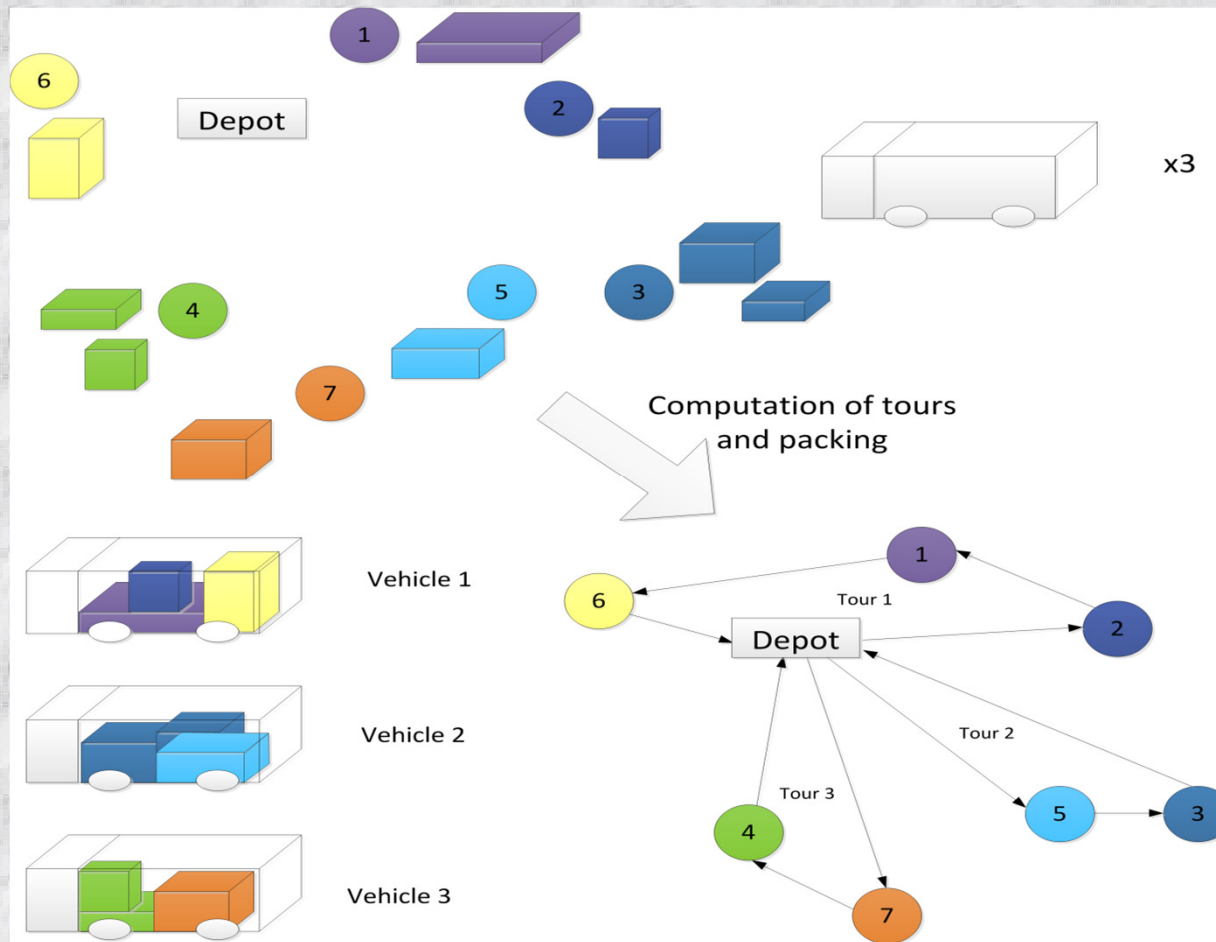
An approach: introducing learning devices (SVM, Neural Network..) in order to deal with the *weak* and *strong* feasibility of 2D and 3D-packing

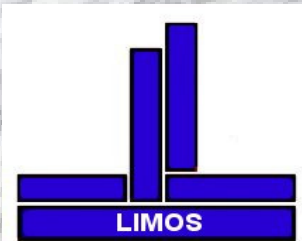
At stake:

- Simultaneously dealing with distinct granularity levels;
- > Getting fast approximation results for complex problems
- Ensuring consistency of linked models -> Getting fast approximation results for complex problems



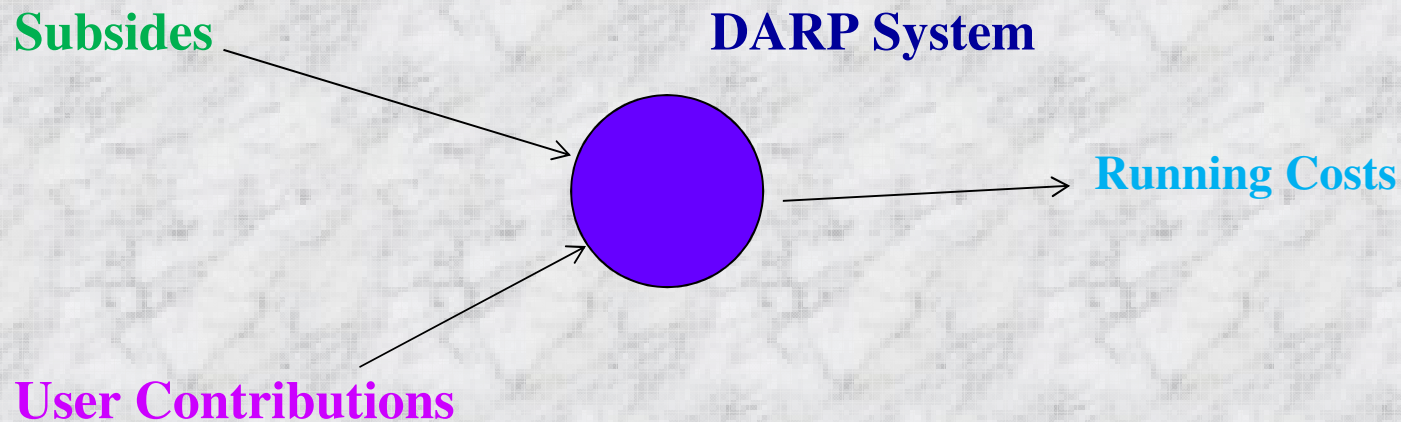
DARP: New Paradigms





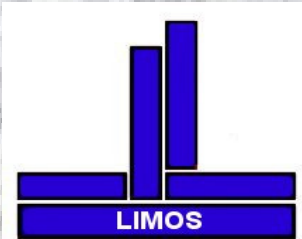
DARP: New Paradigms

Linking Routing/Pricing/Subsidizing.



Routing policy + Expected Demand -> Expected Costs

Prices + Routing Policy -> QoS -> Expected Demand

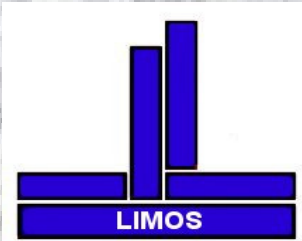


DARP: New Paradigms

Question: **which prices, which subsidies?**

Approach:

- (1). **Cooperative Game Framework** (*Network cooperative Games: Granot, Maschler 1998, Tamir 1993*) *Cooperative Games with Elastic Demands: Bendali, Quilliot 2005* => Avoiding a user subgroup to set its own TAD service
- (2). **Master Slave (bilevel) Decomposition Scheme:**
 - **Main Problem -> Prices**
 - **Slave Problem -> Designing a routing policy for a user subgroup**
 - **Technological Gap: *Evaluating Price/QoS Elasticity of Demand***



DARP: New Paradigms

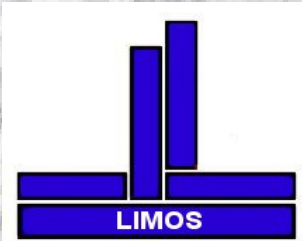
V.2. Non Standard Criteria.

Robustness/Stochastic Complexity.

At stake: Adaptability of the solution when it comes to implementation .

Example: DARP (dynamic/Static) => Current Schedule σ : which ability to take into account future demands, unexpected delays and “rendez-vous” failure?

Difficult problem: Currently suffering from a deficit of formal approach.



DARP: New Paradigms

The basic point: the problem cannot be handled according to its current representation

- **Input data:** must involve a formal and quantified representation of the events: ad hoc language;
- **Output Object:** must take the form of:
 - *A set of constraints and decision rules;*
 - *A strategy (decision tree) on those constraints*

Example: Simple DARP

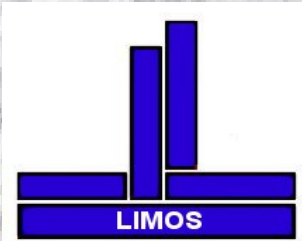
Schedule: a set Λ of additional constraints: (Un)Load(x) precede (Un)Load(y) on vehicle v + implicit priority rule.

Schedule Strategy (mixed schedule): set of **decision rules**.

Rule: Instant t , State S contain pattern E

Finished tasks A , Currently running task $B \models$ Modify Λ

A problem: part the schedule language semantics must be shared by the users.



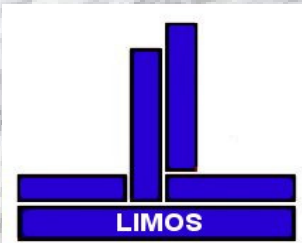
DARP: New Paradigms

Reliability.

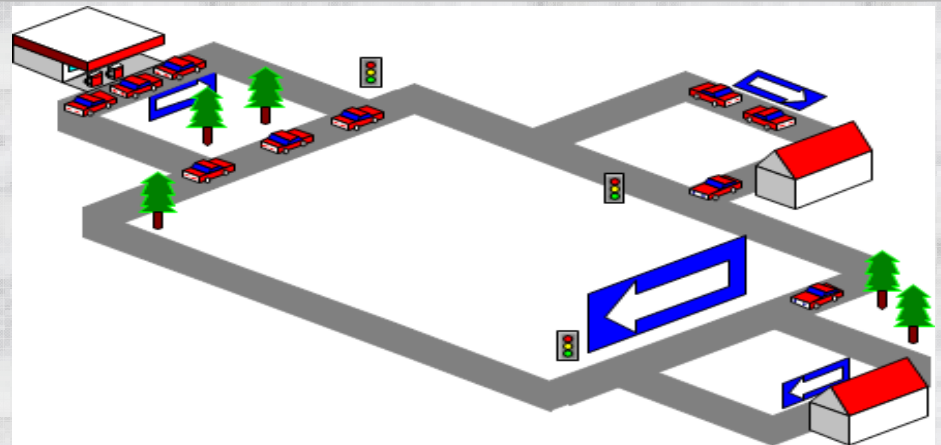
VIPA DARP: Avoiding “hazardeous” manoeuvring: overtaking...,
avoiding schedule modifications

=> Making passenger of a given vehicle share same loading and unloading nodes.

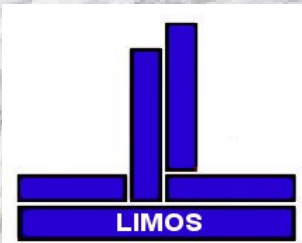
At stake: conveniently modelling reliability in a given monitoring context,
and casting it into the decisional framework .



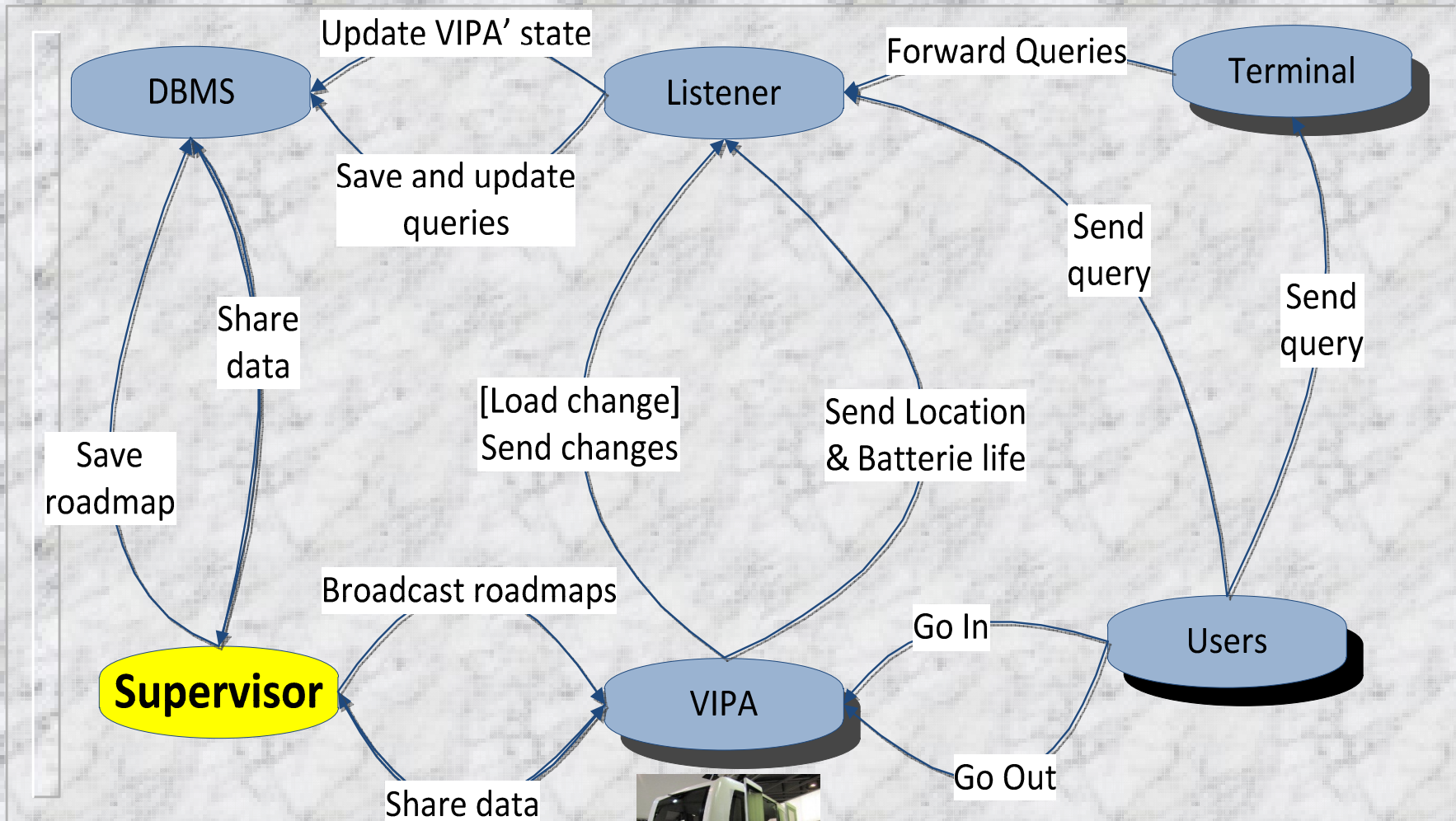
DARP: New Paradigms

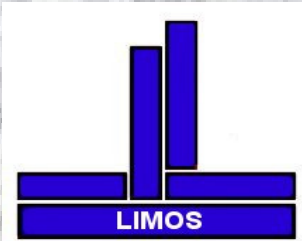


- Stops for users and maintenance
- A one-way loop with outputs for stations
- Homogeneous fleet of autonomous vehicles (VIPA)
- Users ask for a vehicle via mobile phone or a terminal



DARP: New Paradigms





DARP: New Paradigms

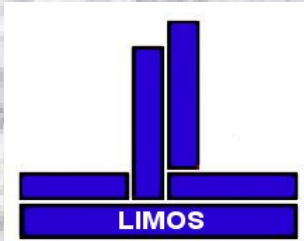
Genericity.

DARP Contexts: Highly Evolutive, Continuum Dynamic/Static

At stake: Development cost, adaptability to model evolution .

Generic Framework?

- *Dynamic Flow/Time Over flow*
- *Ruled Based Systems*
- *Insertion Algorithms...*



DARP: New Paradigms

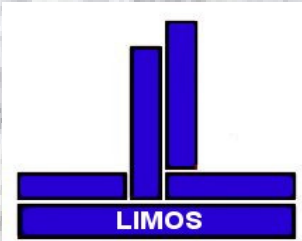
V.3. Non Standard Contexts.

Taking into account technological, organizational, societal context!

Collaborative Planning

The principle: even if you are the “boss”, negotiation is at the heart of any decision process

DARP? The ruler of a DARP service may not be in direct control of all the vehicles involved in the system: mix of AUTOLIB shared vehicle fleet, ad hoc shuttle fleet, “co-transportation” devoted individual cars -> Dependence on the will of other players (subcontractors), which have their own agenda and criteria.



DARP: New Paradigms

An illustration of Collaborative Planning: The Doodle.

A “**master**”, and its partners => May be viewed as a collaborative RCPSP.

Main task: the meeting; Auxiliary tasks: the moves of the partners

Partners are at the same time resources and tasks.

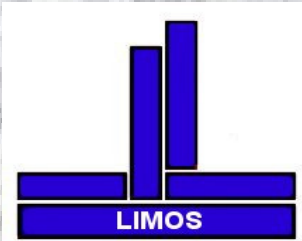
Decision oriented computing devices (and related models):

- A **master** device \mathcal{M} : consider the **constraints** provided by the partners and schedule the meeting;
- Partners devices \mathcal{P}_i , $i = 1..N$: schedule partner i , compute constraints and transmits them to \mathcal{M} ;

Process Main Loop:

\mathcal{P}_i , $i = 1..N$ \leftarrow ----- \rightarrow \mathcal{M} : -> succeed or fail in computing
accept or reject the proposal

The master \mathcal{M} : if failure, ask some of the \mathcal{P}_i , to relax their constraints Else send the proposal to the partners



DARP: New Paradigms

The partners: \mathcal{P}_i , $i = 1..N$:

- If they reject the proposal, send new constraints to \mathcal{M} Else: OK.

Requirements: Design a common constraint language: syntax/semantics

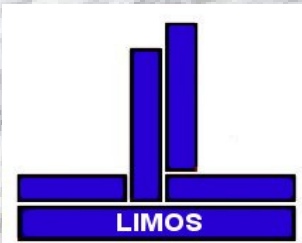
- Design \mathcal{P}_i , in such a way they compute constraints (cf Robustness)
- Handling hidden part...! It is like playing a game. Not everybody want the same thing. Ex: partner j may want the meeting without partner k .

A theoretical framework: Pricing:

- Master M , schedule $\sigma \rightarrow$ Value $V(\sigma)$ resulting from model \mathcal{M} ;
- Partner i , schedule σ , Value $V_i(\sigma)$, resulting from model \mathcal{P}_i ;

Questions:

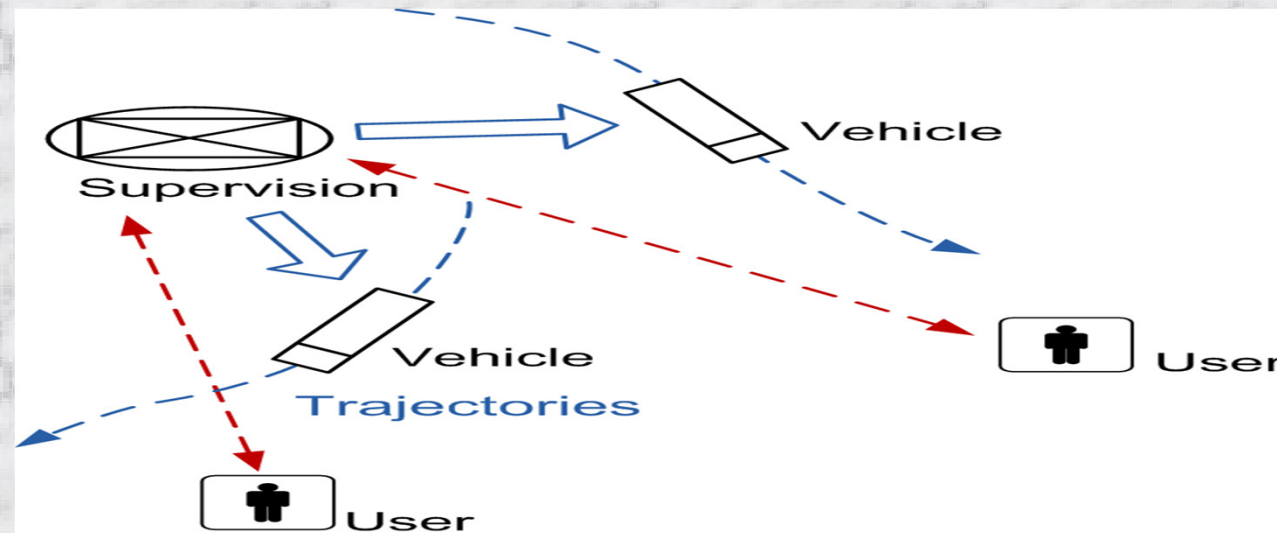
- Which payments between M and its partners in order to make possible reaching a convenient schedule?
 - Cooperative Game Framework (Shapley, Core notion...)
 - Concurrential (non cooperative) framework? (Nash...)



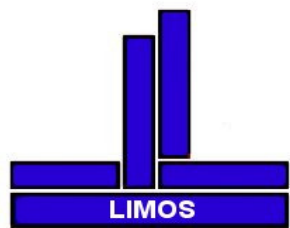
DARP: New Paradigms

Dynamic Scheduling.

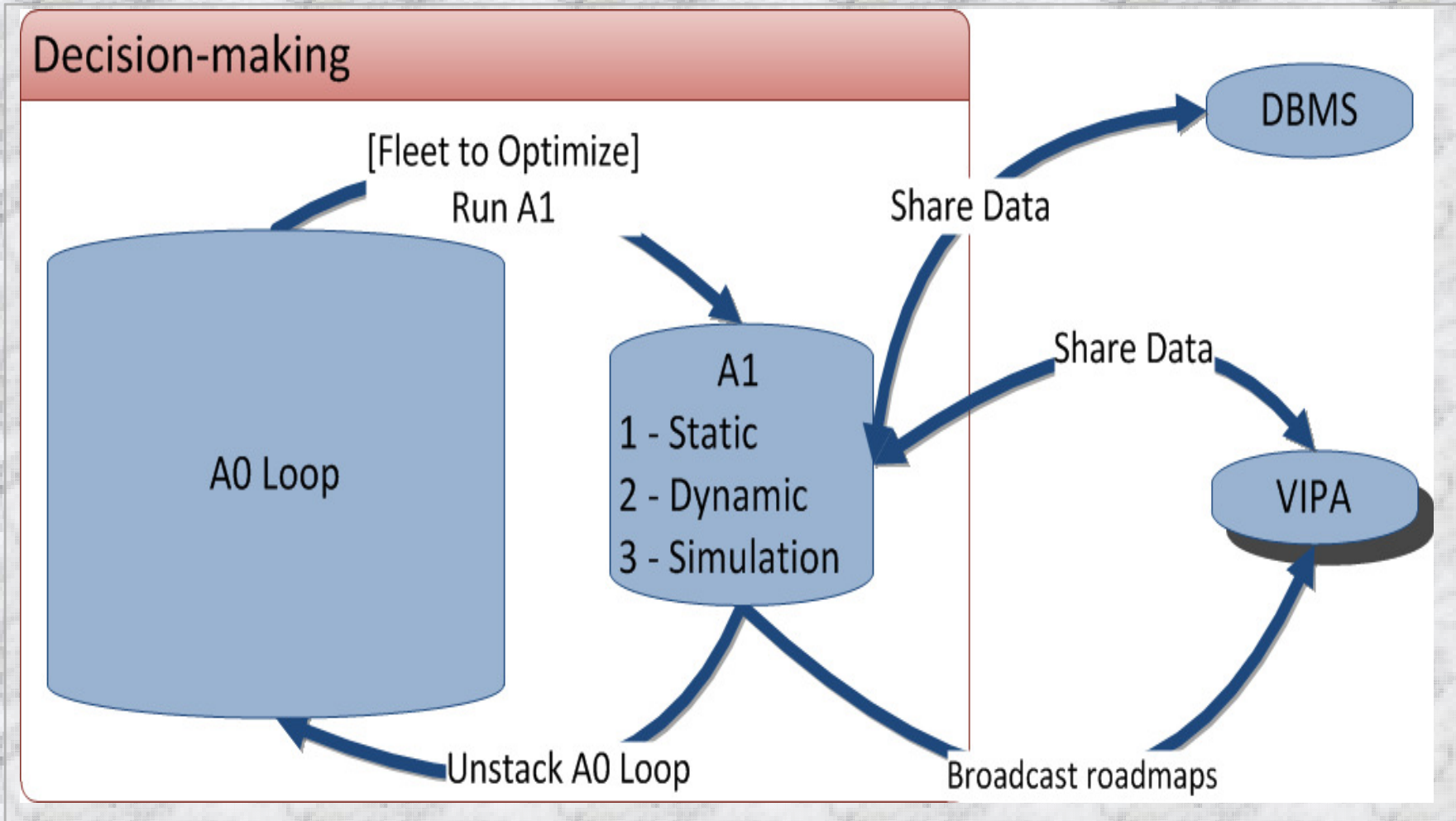
Real Time DARP

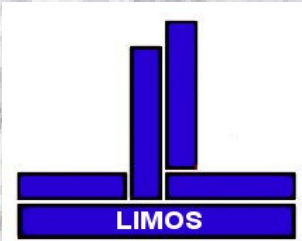


Customer x (tasks) asks for service from origin node $o(x)$ to destination node $d(x)$, while imposing temporal constraints



Innovative Mobility





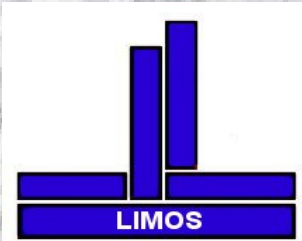
DARP: New Paradigms

Process:

- Between instant t_{n-1} and instant $t = t_n$, customers ask
(the supervisor or some of the vehicles: centralized/decentralized) for service;
- Instant $[t, t+\alpha]$: some activation process \mathcal{A} decide to launch the replanification process \mathcal{P} ,
- Instant $[t+\alpha, t + \alpha + \beta]$: \mathcal{P} compute a new planning for the vehicles, send answers to the customers: meeting proposal or rejection of the demand, and send orders to the vehicles;
- Instant $[t+\alpha+\beta, t_{n+1}]$: vehicles and customers run their way, new demands are registers, as well as failed meetings or rejected proposals.

Requirements:

- Design algorithmic processes A and B; Models: which meaning to “*replanification*”, acceptable for users and communication system
- Acquire and conveniently model input data;
- Evaluate.

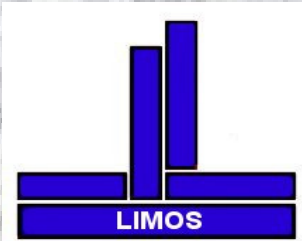


DARP: New Paradigms

The basic points:

- The stochastic dimension of the problem cannot be ignored;
- A priori evaluation must be performed while considering that the input is a stochastic process;
- A posteriori evaluation (test) must be performed through **simulation**;
- The underlying decisional model (module \mathcal{P}) must take into account:
 - *QoS criterion related to the meetings (waiting times...)*
 - *Safety concerns related to communication process between the systems, the vehicles and the customers (ensuring the reliability of the meetings).*

Consequence: the decisional model becomes very different from the static one, and not only a “on line” adaptation of this static model



DARP: New Paradigms

VI. Conclusion.

O.R: a risk of getting old...

New Trends: arise from societal and technological change

But: Tackling new issues requires more than inserting additional constraints and applying old processes.

Smart cities: a very rich play-ground